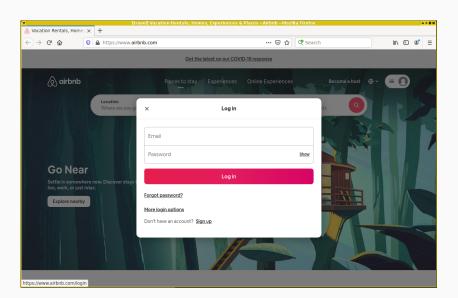
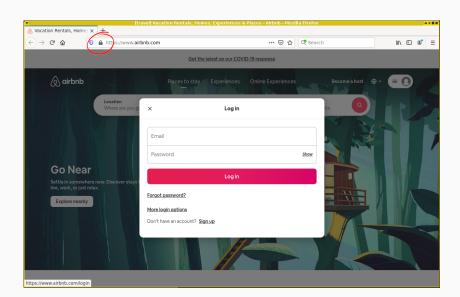
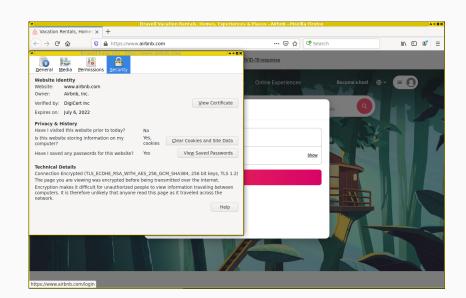


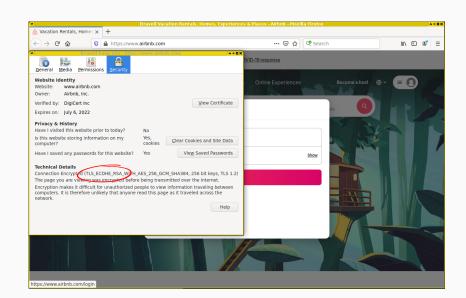
The transition to post-quantum cryptography: challenge and chance

Peter Schwabe November 14, 2020









Polynomial-Time Algorithms for Prime Factorization and Discrete Logarithms on a Quantum Computer*

Peter W. Shor[†]

Abstract

A digital computer is generally believed to be an efficient universal computing device; that is, it is believed able to simulate any physical computing device with an increase in computation time by at most a polynomial factor. This may not be true when quantum mechanics is taken into consideration. This paper considers factoring integers and finding discrete logarithms, two problems which are generally thought to be hard on a classical computer and which have been used as the basis of several proposed cryptosystems. Efficient randomized algorithms are given for these two problems on a hypothetical quantum computer. These algorithms take a number of steps polynomial in the input size, e.g., the number of digits of the integer to be factored.

"In the past, people have said, maybe it's 50 years away, it's a dream, maybe it'll happen sometime. I used to think it was 50. Now I'm thinking like it's 15 or a little more. It's within reach. It's within our lifetime. It's going to happen."

-Mark Ketchen (IBM), Feb. 2012, about quantum computers

Post-quantum crypto

Definition

Post-quantum crypto is (asymmetric) crypto that resists attacks using classical *and quantum* computers.

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5 main directions

- · Lattice-based crypto (PKE and Sigs)
- Code-based crypto (mainly PKE)
- Multivariate-based crypto (mainly Sigs)
- Hash-based signatures (only Sigs)
- Isogeny-based crypto (so far, mainly PKE)

The NIST PQC "not-a-competition"

- Inspired by two earlier NIST crypto competitions:
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 - SHA3, running from 2007 to 2012

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- · Selection through an open process and multiple rounds
- Actual decisions are being made by NIST
- · PQC project:
 - · Announcement: Feb 2016
 - · Call for proposals: Dec 2016 (based on community input)
 - · Deadline for submissions: Nov 2017

The NIST competition: initial overview

Count of Problem Category	Column Labels		
Row Labels	Key Exchange	Signature	Grand Total
?	1		1
Braids	1	1	2
Chebychev	1		1
Codes	19	5	24
Finite Automata	1	1	2
Hash		4	4
Hypercomplex Numbers	1		1
Isogeny	1		1
Lattice	24	4	28
Mult. Var	6	7	13
Rand. walk	1		1
RSA	1	1	2
Grand Total	57	23	80
	1 31		

Overview tweeted by Jacob Alperin-Sheriff on Dec 4, 2017.

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Signature schemes

- · 3 lattice-based
- 2 symmetric-crypto based
- 4 MQ-based

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- 4 key-agreement schemes
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 - · 1 code-based
- · 3 signature schemes
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Alternate schemes

- 5 key-agreement schemes
 - · 2 lattice-based
 - 2 code-based
 - 1 isogeny-based
- 3 signature schemes
 - · 2 symmetric-crypto based
 - 1 MQ-based

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- \approx one year later get standards

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Mission accomplished – The world is safe again!

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... or is it?

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Replacing MD5 was "easy"!

Challenge 1: Performance



- 10% performance difference matters!
 - · Reduce cost for busy servers
 - · Fit into constrained devices





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 - · Fit into constrained devices
- · Small routines executed many times
- Often hand-optimized on assembly level





Challenge 1: Performance (ctd.)

Elliptic-curve cryptography

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- SPHINCS⁺ signing: ≈3 billion cycles
- Kyber (all ops): <80 kcycles
- Kyber data sent: <1.2 KB

Security reductions

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- · proofs may be wrong

The case of OCB2

- 2004: Rogaway proposes OCB2
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Some NIST PQC proof failures

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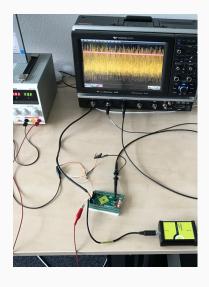
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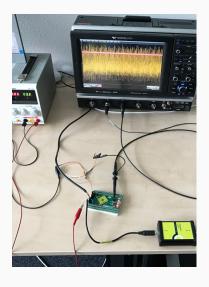
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- Round-2 qTesla proof wrong (?) ⇒ devastating attack

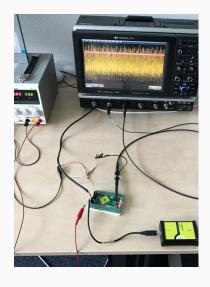




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- · Side-channel attacks:
 - Measure information
 - · Use to obtain secret data
- Timing attacks can be done remotely
- Cost of countermeasures heavily depends on the scheme

"the implementation security aspect of lattice-based cryptography is still a vastly unexplored and open topic"

- Primas, Pessl, Mangard, 2017.

"...this isn't very different for any of the other areas of post-quantum crypto"

- Schwabe, 2020.

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For many applications, implementations are not ready.

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- Hash-based signatures XMSS and LMS

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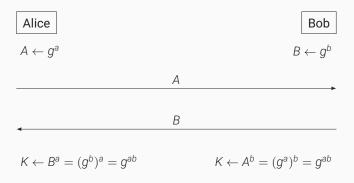
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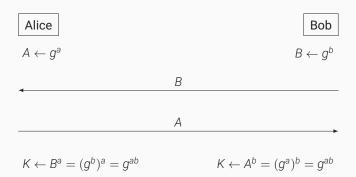
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"It's a huge foot cannon" — Adam Langley

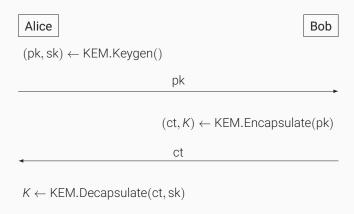
Challenge 5: The curious case of Diffie-Hellman



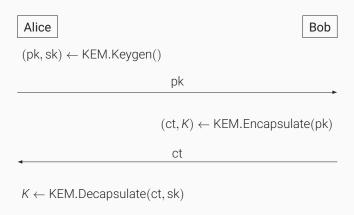
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KEMs: as close as you'll get to DH



KEMs: as close as you'll get to DH*



^{*}Except with CSIDH (Castryck, Lange, Martindale, Renes, Panny, 2018)

Is it already too late?

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- When do we need to start migrating?

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- Consider the following attack against confidentiality
 - Record encrypted message today
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- · When do we need to start migrating?
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How long do we need today's communication to be secure?

How long does it take us to migrate?

But for signatures we have time, right?

- · Signatures provide authentication
- · Cannot retroactively "decrypt" anything
- Stop accepting pre-quantum signatures once there is a quantum computer

But for signatures we have time, right?

- · Signatures provide authentication
- · Cannot retroactively "decrypt" anything
- Stop accepting pre-quantum signatures once there is a quantum computer
- · May need to prepare devices today!
- · Signatures are used for, e.g., software updates
- · What if I cannot update anymore in 15 years?
 - · What's the lifetime of a car?
 - What's the lifetime of smart-home appliances?

A chance?

How can this migration be a *chance*?

PlayStation 3 hack - how it happened and what it means











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Careful: high-assurance does not mean "unbreakable"

Formal = machine readable

HACS success stories



HACS success stories



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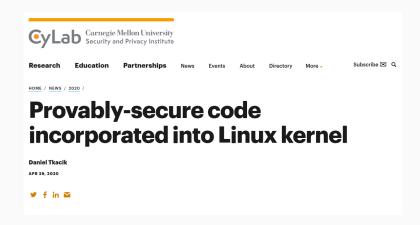
Automated cryptocode generator is helping secure the web

System automatically writes optimized algorithms to encrypt data in Google Chrome browsers and web applications.

Rob Matheson | MIT News Office June 17, 2019



HACS success stories



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Yes, this is overly optimistic.

...let's see it as an ambitious goal!

Some pointers

PQC resources

- NIST PQC website: https://csrc.nist.gov/Projects/Post-Quantum-Cryptography
- NIST mailing list: https://csrc.nist.gov/projects/post-quantum-cryptography/ email-list https://groups.google.com/a/list.nist.gov/g/pqc-forum
- Open Quantum Safe https://openquantumsafe.org/
- PQC Wiki: https://pqc-wiki.fau.edu

HACS resources

• HACS workshop: https://www.hacs-workshop.org/