

### Some lessons learned from NIST PQC

Peter Schwabe

April 23, 2025

- Based on invited talk at PQCRYPTO 2022
- Not much on signature on-ramp

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  - · What went well
  - · What went not so well

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- Looking back after 9 years of NIST PQC:
  - · What went well
  - What went not so well (in "our submissions")

### Our submissions

#### CRYSTALS-Kyber

Roberto Avanzi

Joppe Bos

Jintai Ding

Léo Ducas

Eike Kiltz

Tancrède Lepoint

Vadim Lyubashevsky

John M. Schanck

Peter Schwabe

Gregor Seiler

Damien Stehle

#### CRYSTALS-Dilithium

Léo Ducas Fike Kiltz

Tancrède Lepoint

Vadim Lyubashevsky

Peter Schwabe

Gregor Seiler

Damien Stehlé

Shi Bai

#### SPHINCS+

Jean-Philippe Aumasson

Daniel J. Bernstein

Ward Beullens

Christoph Dobraunig

Maria Eichlseder

Scott Fluhrer

Stefan-Lukas Gazdag

Andreas Hülsing

Panos Kampanakis

Stefan Kölbl

Tanja Lange

Martin M. Lauridsen

Florian Mendel

Ruben Niederhagen

Christian Rechberger

Joost Rijneveld Peter Schwahe

Bas Westerbaan

### 1. Designing

"A complete written specification of the algorithms shall be included, consisting of all necessary mathematical operations, equations, tables, diagrams, and parameters that are needed to implement the algorithms. The document shall include design rationale and an explanation for all the important design decisions that are made"

-Dustin Moody, February 24, 2016 (PQCRYPTO 2016)

"Oh, you mean numbers?!"

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- Choose concrete parameters for different security levels
- All randomness from randombytes or just a seed?
- Fix sampling algorithms (e.g., constant-time sorting)
- Select symmetric primitives
- Concretize domain separation

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- Choose concrete parameters for different security levels
- All randomness from randombytes or just a seed?
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- Select symmetric primitives
- Concretize domain separation
- Tradeoffs, tradeoffs, tradeoffs. . .

### 1. Designing – Exhibit A

#### Dilithium - v3.0 vs. v3.1

$$\begin{array}{l} \underline{\mathsf{Sign}(sk,M)} \\ \underline{\mathsf{09}} \ \mathbf{A} \in R_q^{k \times \ell} \coloneqq \mathsf{ExpandA}(\rho) \\ \underline{\mathsf{10}} \ \mu \in \{0,1\}^{384} \coloneqq \mathsf{CRH}(tr \parallel M) \\ \underline{\mathsf{11}} \ \kappa := 0, \ (\mathbf{z},\mathbf{h}) := \bot \end{array}$$

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- · Message hash only 384 bits
- 192 bits of sec. against collisions
- Not sufficient for NIST level 5

# 1. Designing – Exhibit B

#### SPHINCS<sup>+</sup>, round 3

- Security relies on DM-SPR (Distinct-function multi-target second preimage resistance) of underlying hash function
- Three different choices of hash function: SHA-256, SHAKE-256, Haraka

# 1. Designing – Exhibit B

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- Attack cost higher than NIST level 1, but lower than level 3 and 5

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"This is an interesting attack that does demonstrate that our real hash functions do not perfectly behave like random oracles"

-Andreas Hülsing, April 21, 2022

1. Will the schemes selected now be widely used?

2. Will those schemes survive in the long run?

### Deployment of ML-KEM

- Integrated into Firefox, Chrome, Brave...
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### Deployment of ML-DSA and SLH-DSA

- SLH-DSA for secure boot on OpenTitan
- First cars with ML-DSA-secured software updates soon

### 2. Proving

"Submitters are not required to provide a proof of security, although such proofs will be considered if they are available."

-NIST PQC, Call for Proposals

# 2. Proving – Exhibit A

### Kyber round 1

- LPR scheme's public key is  $\mathbf{t} = \mathbf{A}\mathbf{s} + \mathbf{e}$
- This is an (R/M)LWE sample and assumed to be uniform in the proof

# 2. Proving – Exhibit A

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- Kyber in round 1 compressed this (round off low bits)
- $\mathbf{t}' = \mathsf{Decompress}(\mathsf{Compress}(\mathbf{t}))$  is **not** uniform

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- Kyber in round 1 compressed this (round off low bits)
- $\mathbf{t}' = \mathsf{Decompress}(\mathsf{Compress}(\mathbf{t}))$  is **not** uniform
- Reduction from MLWE in round-1 Kyber was invalid:

"We note that a potential issue is that the security proof does not directly apply to Kyber itself, but rather to a modified version of the scheme which does not compress the public key."

-NIST IR 8240

### 2. Proving – Exhibit B

#### SPHINCS+ - original proof

- Reduce from second-preimage resistance
- Place challenge x = H(y) inside hash chains
- Forgery produces preimage of x with certain prob.
- Reduction hopes to obtain second preimage  $y' \neq y$  with x = H(y')

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- Problem: len(x) = len(y)
- Second preimage does not exist with high probablity
- Forger can refuse to forge if there is a second preimage

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- · Proof doesn't apply to the scheme
- · Proof correct, but theorem "insufficient"
  - · Example: attack hides in non-tightness
- Proof (and possibly theorem) too vague
- Theorem and proof correct, but not very useful
  - "A is secure if A is secure"

### 3. Implementing

"NISTPQC, despite being an important and timely project, has produced the largest regression **ever** in the quality of cryptographic software. This will not be easy to fix."

-Daniel J. Bernstein, October 5, 2018

#### Dilithium commit on Dec. 28, 2017

```
212
                  t = buf[pos];
213
                  t |= (uint32_t)buf[pos + 1] << 8;
214
                  t |= (uint32_t)buf[pos + 2] << 16;
215
                 t &= 0xFFFFF;
                 to = buf[pos];
      337
      338
                 t0 |= (uint32_t)buf[pos + 1] << 8;
                  t0 |= (uint32_t)buf[pos + 2] << 16;
       339 +
                  to &= 0xFFFFF:
       340 +
216
      341
217
                  t = buf[pos + 2] >> 4:
218
                  t |= (uint32_t)buf[pos + 3] << 4;
                  t |= (uint32 t)buf[pos + 4] << 12;
219
      342 +
                 t1 = buf[pos + 2] >> 4;
                 t1 |= (uint32_t)buf[pos + 3] << 4;
       343 +
                  t1 |= (uint32 t)buf[pos + 4] << 12;
      344 +
```

- · Bug in Dilithium sampler
- Two consecutive coefficients are equal
- Allows key recovery
- Reported by Peter Pessl on Dec. 27, 2017

#### **PQClean**

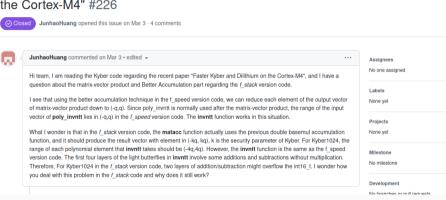
- Joint work with Matthias Kannwischer, Joost Rijneveld, John Schanck, Douglas Stebila, Goutam Tamvada, Thom Wiggers
- Test harness for PQC implementations
- Integrate reference implementations
  - Run through test harness
  - "clean up"

Flaw	KEMs	Sigs	Flaw	KEMs	Sigs
Memory safety	3	4	Endianness assumptions	7	2
Signed integer overflow	3	1	Platform-specific behavior	4	0
Alignment assumptions	4	4	Variable-Length Arrays	4	1
Other Undefined Behavior	1	1	Compiler extensions	5	2
Dead code	3	4	Integer sizes	6	3
Global state	2	1	Non-constant time	4	0
Licensing unclear	3	1			

"In almost every scheme we identified "unclean" code, ranging from missing casts to memory safety problems and other forms of undefined behavior."

-https://eprint.iacr.org/2022/337

# Questions about the range analysis of iNTT for "Faster Kyber and Dilithium on the Cortex-M4" #226



"...two layers of addition/subtraction might overflow the int16\_t. I wonder how you deal with this problem in the f\_stack code and why does it still work?"

"...two layers of addition/subtraction might overflow the int16\_t. I wonder how you deal with this problem in the f\_stack code and why does it still work?"

"...On your question on why it still works, I believe that this is an edge case that does not get triggered by the testing scripts."



#### 4. Benchmarking

#### Two main benchmarking frameworks

- eBACS/SUPERCOP(https://bench.cr.yp.to)
  - · Run by Bernstein and Lange
  - Overlap with submissions: Classic McEliece, NTRU Prime, PQ-RSA, SPHINCS+
  - Benchmark on variety of "large" platforms
  - · Need to run Linux/UNIX OS

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  - Benchmark on variety of "large" platforms
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- pqm4 (https://github.com/mupq/pqm4)
  - · Run by Kannwischer, Petri, Rijneveld, Schwabe, Stoffelen
  - Overlap with submissions: Classic McEliece, Kyber, Dilithium, NTRU, MQDSS, NewHope, SPHINCS<sup>+</sup>, MAYO, UOV
  - Benchmark on Arm Cortex M4

#### Lack of independent benchmarking

- Benchmarking in the hands of submitters
- Much more desirable: Independent benchmarking by competition "hosts"

#### APIs matter

- NIST-API: serialization part of keypair, encaps, decaps, sign, sign\_open
- · Deployments use API with seperate serialization
  - · Ephemeral deployments never serialize secret keys
  - · Static deployments amortize de-serialization
- Massive impact on performance and design choices!

#### Consider HW acceleration for symmetric crypto

- Many PQC schemes bottlenecked by Keccak
- Example: ML-KEM-768 encapsulation on OpenTitan<sup>1</sup>
  - Software Keccak takes 66% of total cycles
  - · With hardware acceleration: 3% of total cycles

<sup>&</sup>lt;sup>1</sup>A. Abdulrahman, F. Oberhansl, H. Pham, J. Philipoom, P. Schwabe, T. Stelzer, A. Zankl. *Towards ML-KEM & ML-DSA on OpenTitan*, IEEE S&P 2025, to appear

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- Example: ML-KEM-768 encapsulation on OpenTitan<sup>1</sup>
  - Software Keccak takes 66% of total cycles
  - · With hardware acceleration: 3% of total cycles
- · Recommendation: benchmark also with HW Keccak, AES, SHA-2, SM3, SM4, ZUC
- Alternative: use very fast fake symmetric crypto for benchmarks

<sup>&</sup>lt;sup>1</sup>A. Abdulrahman, F. Oberhansl, H. Pham, J. Philipoom, P. Schwabe, T. Stelzer, A. Zankl. *Towards ML-KEM & ML-DSA on OpenTitan*, IEEE S&P 2025, to appear

## 5. Attacking

"The idea is that participants put their algorithms into the ring, and then we all spend a few years beating on each other's submissions."

-Bruce Schneier, August 8, 2022

#### 5. Attacking – Guessed Once

```
def recover_bit(ct, bit):
    assert bit < len(ct) // 4000
    ts = [struct.unpack('BB', ct[i:i+2]) for i in range(4000*bit, 4000*(bit+1), 2)]
    xs, ys = [a for a, b in ts if b == 1], [a for a, b in ts if b == 2]
    return sum(xs) / len(xs) >= sum(ys) / len(ys)

def decrypt(ct):
    res = sum(recover_bit(ct, b) << b for b in range(len(ct) // 4000))
    return int.to_bytes(res, len(ct) // 4000 // 8, 'little')</pre>
```

-Lorenz Panny, December 21, 2017

ia.cr/2022/975

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- Competent, smart people tried to break it (e.g., Martindale, Panny: How to not break SIDH (ePrint 2019/558))

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- Competent, smart people tried to break it (e.g., Martindale, Panny: How to not break SIDH (ePrint 2019/558))

Yet, full break without any "warning"

# 5. Attacking – even more attacks!



### 6. Communicating

"I don't know if you're familiar with this website, twitter.com? If you like crypto drama, this is where you go. Except if you go to the pqc-forum, which is also... generally... it's even better".

-Bor de Kock, August 17, 2022

### 6. Communicating

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https://www.youtube.com/watch?v=kXcYy8L0I9s, starting at 20:22.

"Follow the "Rule of 1" and the "Rule of n": When you speak, make 1 point and then let others speak, and when in a group of "n" people, speak "1/nth" of the time."

Aspiration Participants: Guidelines

 $\verb|https://facilitation.aspirationtech.org/index.php?title=Participants:Guidelines||$ 

Download all mails, run statistics

Download almost all mails, run statistics

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- pqc-forum had 666 threads ("conversations") on Sep. 14, 2022
- First mail by Dustin Moody from Aug. 1, 2016
- I have 2805 mails (first one from Nov. 2, 2016)

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```
for i in mails/*;do
   FROM=$(grep ^From: $i | head -n 1 | sed "s/From:\ //" | sed "s/.*<\([^>]*\)>/\1/")
   if [ "$FROM" = "pqc-forum@list.nist.gov" ]; then
      FROM=$(grep ^X-Original-From: $i | head -n 1 | \
            sed "s/X-Original-From:\ //" | sed "s/.*<\([^>]*\)>/\1/")
   fi
   echo $FROM
done | sort | uniq -c | sort -n
```

- 369 sender addresses
- Sometimes multiple addresses for one person
- 131 addresses sent just one mail
- 275 addresses sent at most 5 mails

#### The "Top 10"

address1		407
address2		146
address3		113
address4		106
address5		100
address6		81
address7		69
address8		68
address9		50
address10		47
address11		47
	address2 address3 address4 address5 address6 address7 address8 address9 address10	address2 address3 address4 address5 address6 address7 address8 address9 address10

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1.	address1	407
2.	dustin.moody@nist.gov	146
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>50% of mails sent by only 15 people.

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>50% of mails sent by only 15 people.

>30% of all words by non-NIST authors are from one address.

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- 2. Use mechanized proof techniques as early and extensively as possible
- 3. Real-world test deployments as early as possible
- 4. Use a different communication platform than Google Groups
- 5. Enjoy the ride and be nice to each other!