The migration to post-quantum cryptography

Peter Schwabe

Max Planck Institute for Security and Privacy

October 9, 2025



[A small demo]



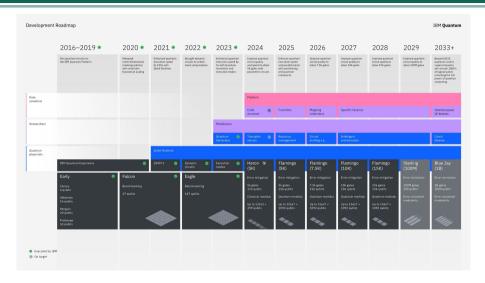
Polynomial-Time Algorithms for Prime Factorization and Discrete Logarithms on a Quantum Computer*

Peter W. Shor[†]

Abstract

A digital computer is generally believed to be an efficient universal computing device; that is, it is believed able to simulate any physical computing device with an increase in computation time by at most a polynomial factor. This may not be true when quantum mechanics is taken into consideration. This paper considers factoring integers and finding discrete logarithms, two problems which are generally thought to be hard on a classical computer and which have been used as the basis of several proposed cryptosystems. Efficient randomized algorithms are given for these two problems on a hypothetical quantum computer. These algorithms take a number of steps polynomial in the input size, e.g., the number of digits of the integer to be factored.





Post-quantum crypto (PQC)



Definition

Post-quantum crypto is (asymmetric) crypto that resists attacks using classical and quantum computers.

Post-quantum crypto (PQC)



Definition

Post-quantum crypto is (asymmetric) crypto that resists attacks using classical and quantum computers.

5 main directions

- ► Lattice-based crypto (PKE and Sigs)
- ► Code-based crypto (mainly PKE)
- Multivariate-based crypto (mainly Sigs)
- ► Hash-based signatures (only Sigs)
- Isogeny-based crypto (it's complicated...)

Should you care now?

"Harvest now, decrypt later"



https://en.wikipedia.org/wiki/Utah_Data_Center#/media/File:EFF_photograph_of_NSA's_Utah_Data_Center.jpg

Should you care now?

"Harvest now, decrypt later"





 $https://en.wikipedia.org/wiki/Utah_Data_Center\#/media/File: EFF_photograph_of_NSA's_Utah_Data_Center.jpg$

Mosca's theorem

$$X + Y > Z$$

- ► X: For how long do you need encrypted data to be secure?
- ► Y: How long does it take you to migrate to PQC
- ► Z: Time it will take to build a cryptographically relevant quantum computer

If
$$X + Y > Z$$
, you should worry.

NIST PQC – how it started



Count of Problem Category	Column Labels		
Row Labels	Key Exchange	Signature	Grand Total
?	1		1
Braids	1	1	2
Chebychev	1		1
Codes	19	5	24
Finite Automata	1	1	2
Hash		4	4
Hypercomplex Numbers	1		1
Isogeny	1		1
Lattice	24	4	28
Mult. Var	6	7	13
Rand. walk	1		1
RSA	1	1	2
Grand Total	57	23	80
Q 4	1 31		

Overview tweeted by Jacob Alperin-Sheriff on Dec 4, 2017.

NIST PQC – how it went



NIST PQC

Nov. 2017
69 proposals

Round 1
Feb. 2019
26 proposals

Round 2
7+8 proposals

Round 3
7+8 proposals

Guil. 2020
4 "winners"

NIST PQC – how it went





"The public-key encryption and key-establishment algorithm that will be standardized is CRYSTALS-KYBER. The digital signatures that will be standardized are CRYSTALS-Dilithium, FALCON, and SPHINCS⁺. While there are multiple signature algorithms selected, NIST recommends CRYSTALS-Dilithium as the primary algorithm to be implemented"



[Back to our demo]



So, all good? Is the world safe again?



- ► MD5 is a cryptographic hash function
- ► Hash functions are used as building blocks all over the place



- ► MD5 is a cryptographic hash function
- ► Hash functions are used as building blocks all over the place
- ▶ 1991: MD5 is proposed by Rivest



- ► MD5 is a cryptographic hash function
- ► Hash functions are used as building blocks all over the place
- ▶ 1991: MD5 is proposed by Rivest
- ▶ 1993: Collisions in MD5 compression function (den Boer, Bosselaers)



- ► MD5 is a cryptographic hash function
- ► Hash functions are used as building blocks all over the place
- ▶ 1991: MD5 is proposed by Rivest
- ▶ 1993: Collisions in MD5 compression function (den Boer, Bosselaers)
- ▶ 1996: Dobbertin, Bosselaers, Preneel: concerns about MD5



- ► MD5 is a cryptographic hash function
- ► Hash functions are used as building blocks all over the place
- ▶ 1991: MD5 is proposed by Rivest
- ▶ 1993: Collisions in MD5 compression function (den Boer, Bosselaers)
- ▶ 1996: Dobbertin, Bosselaers, Preneel: concerns about MD5
- 2004: Wang presents MD5 collisions



- ► MD5 is a cryptographic hash function
- ► Hash functions are used as building blocks all over the place
- ▶ 1991: MD5 is proposed by Rivest
- 1993: Collisions in MD5 compression function (den Boer, Bosselaers)
- ▶ 1996: Dobbertin, Bosselaers, Preneel: concerns about MD5
- ▶ 2004: Wang presents MD5 collisions
- 2008: Rogue CA certificate using MD5 (Sotirov, Stevens, Appelbaum, Lenstra, Molnar, Osvik, de Weger)



- ► MD5 is a cryptographic hash function
- ► Hash functions are used as building blocks all over the place
- ▶ 1991: MD5 is proposed by Rivest
- 1993: Collisions in MD5 compression function (den Boer, Bosselaers)
- ▶ 1996: Dobbertin, Bosselaers, Preneel: concerns about MD5
- 2004: Wang presents MD5 collisions
- 2008: Rogue CA certificate using MD5 (Sotirov, Stevens, Appelbaum, Lenstra, Molnar, Osvik, de Weger)
- ▶ 2012: Flame malware exploits MD5 weaknesses



- ► MD5 is a cryptographic hash function
- ► Hash functions are used as building blocks all over the place
- ▶ 1991: MD5 is proposed by Rivest
- ▶ 1993: Collisions in MD5 compression function (den Boer, Bosselaers)
- ▶ 1996: Dobbertin, Bosselaers, Preneel: concerns about MD5
- ▶ 2004: Wang presents MD5 collisions
- 2008: Rogue CA certificate using MD5 (Sotirov, Stevens, Appelbaum, Lenstra, Molnar, Osvik, de Weger)
- ▶ 2012: Flame malware exploits MD5 weaknesses

Replacing MD5 was "easy"!

Challenge 1: Performance



X25519 speed

- ► keygen: 28187 Skylake cycles
- ▶ shared: 87942 Skylake cycles

Kyber-768 speed

- ► keygen: 39750 Skylake cycles
- encaps: 53936 Skylake cycles
- ► decaps: 42339 Skylake cycles

Challenge 1: Performance



X25519 speed

- ► keygen: 28187 Skylake cycles
- ► shared: 87942 Skylake cycles

Kyber-768 speed

- ► keygen: 39750 Skylake cycles
- encaps: 53936 Skylake cycles
- ► decaps: 42339 Skylake cycles

X25519 sizes

public key: 32 bytes

Kyber-768 sizes

- ▶ public key: 1184 bytes
- ciphertext: 1088 bytes

Challenge 2: A KEM is not DH!



Alice

$$A \leftarrow q^a$$

Bob

$$B \leftarrow g^b$$

B

$$K \leftarrow B^a = (g^b)^a = g^{ab}$$

$$K \leftarrow A^b = (g^a)^b = g^{ab}$$

Challenge 2: A KEM is not DH!



$$A \leftarrow q^a$$

$$B \leftarrow g^b$$

B

$$K \leftarrow B^a = (g^b)^a = g^{ab}$$

$$K \leftarrow A^b = (g^a)^b = g^{ab}$$

Challenge 2: A KEM is not DH!



Initiator

Responder

$$(pk, sk) \leftarrow KEM.Gen$$

pk

$$(\mathsf{ct}, K) \leftarrow \mathsf{KEM}.\mathsf{Enc}(\mathsf{pk})$$

ct

$$K \leftarrow \mathsf{KEM.Dec}(\mathsf{ct}, \mathsf{sk})$$



Dilithium commit on Dec. 28, 2017

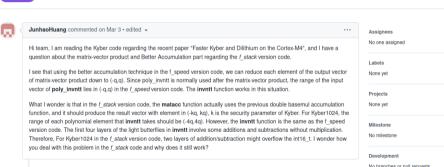
```
212
                 t = buf[pos];
                 t |= (uint32_t)buf[pos + 1] << 8;
213
214
                 t |= (uint32_t)buf[pos + 2] << 16;
215
                 t &= 0xFFFFF;
      337
                 t0 = buf[pos];
      338 + t0 |= (uint32 t)buf[pos + 1] << 8;
      339 + t0 |= (uint32_t)buf[pos + 2] << 16;
      340 +
                 to &= 0xFFFFF:
      341
217
                 t = buf[pos + 2] >> 4;
                 t |= (uint32_t)buf[pos + 3] << 4;
218
219
                 t |= (uint32_t)buf[pos + 4] << 12;
                 t1 = buf[pos + 2] >> 4;
      342 +
      343 + t1 |= (uint32 t)buf[pos + 3] << 4;
                 t1 |= (uint32 t)buf[pos + 4] << 12;
      344 +
```

- ► Bug in Dilithium sampler
- ► Two consecutive coefficients are equal
- Allows key recovery
- Reported by Peter Pessl on Dec. 27, 2017



Questions about the range analysis of iNTT for "Faster Kyber and Dilithium on the Cortex-M4" #226

○ Closed JunhaoHuang opened this issue on Mar 3 · 4 comments





"...two layers of addition/subtraction might overflow the int16_t. I wonder how you deal with this problem in the f_stack code and why does it still work?"



"... two layers of addition/subtraction might overflow the int16_t. I wonder how you deal with this problem in the f_stack code and why does it still work?"

"...On your question on why it still works, I believe that this is an edge case that does not get triggered by the testing scripts."





vincentvbh commented on Mar 6, 2021

Contributor Author ...

There is a bug in the inverse of NTT in Saber. But the bug is triggered with a very low probability that it is not triggered on testing.





Both NTT bugs found by Yang, Liu, Shi, Hwang, Tsai, Wang, and Seiler (TCHES 2022/4)

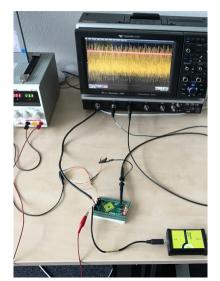
Challenge 4: Implementation Security





Challenge 4: Implementation Security





- Attackers see more than input/output:
 - Power consumption
 - Electromagnetic radiation
 - Timing
- Side-channel attacks:
 - Measure information
 - Use to obtain secret data

Challenge 4: Side-channel countermeasures



Hardware side-channels

- ► Require physical access to device
- Examples: Power, EM attacks
- Protection through dedicated countermeasures
- Typical slowdown of much more than 100%
- Progress, but no "conclusion"; we don't know how to protect PQC!

Challenge 4: Side-channel countermeasures



Hardware side-channels

- ► Require physical access to device
- Examples: Power, EM attacks
- Protection through dedicated countermeasures
- Typical slowdown of much more than 100%
- Progress, but no "conclusion"; we don't know how to protect PQC!

Software side-channels

- ► Leak through microarchitectural side-channels
- No physical access required, can run remotely
- Traditional countermeasure: constant-time
 - ► No branching on secrets
 - No memory access at secret location
 - ▶ No variable-time arithmetic on secrets.

An arms race with compilers



"KyberSlash"

```
t = (((t << 1) + KYBER_Q/2)/KYBER_Q) & 1;
```

- ▶ Division by constant *usually* turns into multiplications
- ► Turns into DIV instructions for certain compiler flags
- ► DIV with secret divident leaks

Compiler (re-)introduced secret branch

```
for(j=0;j<8;j++) {
  mask = -(int16_t)((msg[i] >> j)&1);
  r->coeffs[8*i+j] = mask & ((KYBER_Q+1)/2);
}
```

- ► Carefully hand-crafted to avoid secret branch
- ► Secret branch re-introduced by clang ≥15

Advanced microarchitectural attacks



High-assurance PQC





- ► Effort to **formally verify** crypto
- ► Currently three main projects:
 - EasyCrypt proof assistant
 - jasmin programming language
 - ► Libjade (PQ-)crypto library
- ► Core team of \approx 30–40 people
- ► Discussion forum with >350 people































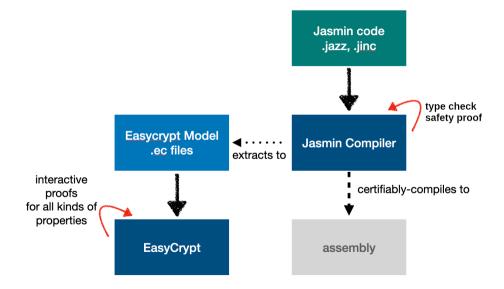






The toolchain and workflow





End-to-end formally verified ML-KEM



- ► Reference and AVX2-optimized implementations in Jasmin
- ► Proven (memory-/type-)safety of implementations
- ► Future-proof constant-time (using Intel's DOIT)
- Principled erasure of sensitive stack/register data at termination
- Systematic protections against Spectre v1
- (Extension to all Spectre variants needs merging)

End-to-end formally verified ML-KEM



- ► Reference and AVX2-optimized implementations in Jasmin
- ► Proven (memory-/type-)safety of implementations
- Future-proof constant-time (using Intel's DOIT)
- Principled erasure of sensitive stack/register data at termination
- Systematic protections against Spectre v1
- (Extension to all Spectre variants needs merging)
- ML-KEM specification in EasyCrypt
- Implementations proven functionally correct (EasyCrypt)
- Reductionist proof of IND-CCA security (EasyCrypt)

End-to-end formally verified ML-KEM



- ► Reference and AVX2-optimized implementations in Jasmin
- Proven (memory-/type-)safety of implementations
- ► Future-proof constant-time (using Intel's DOIT)
- Principled erasure of sensitive stack/register data at termination
- Systematic protections against Spectre v1
- ► (Extension to all Spectre variants needs merging)
- ML-KEM specification in EasyCrypt
- Implementations proven functionally correct (EasyCrypt)
- Reductionist proof of IND-CCA security (EasyCrypt)
- Ongoing work: wrap in ML-KEM "crypto agent"
- Ongoing work: real-world production deployment

https://github.com/pq-code-package/mlkem-libjade

Learn more



NIST PQC

- ► NIST PQC website: https://csrc.nist.gov/Projects/Post-Quantum-Cryptography
- ► NIST mailing list: https://csrc.nist.gov/projects/post-quantum-cryptography/email-list https://groups.google.com/a/list.nist.gov/g/pqc-forum

Formosa Crypto

- ► Main website: https://formosa-crypto.org
- ► Team chat: https://formosa-crypto.zulipchat.com/

Learn even more



Papers related to high-assurance ML-KEM (1/2)

- ► Almeida, Barbosa, Barthe, Grégoire, Laporte, Léchenet, Oliveira, Pacheco, Quaresma, Schwabe, Séré, and Strub. Formally verifying Kyber Episode IV: Implementation Correctness. CHES 2023. https://eprint.iacr.org/2023/215
- Almeida, Arranz Olmos, Barbosa, Barthe, Dupressoir, Grégoire, Laporte, Léchenet, Low, Oliveira, Pacheco, Quaresma, Schwabe, and Strub. Formally verifying Kyber Episode V: Machine-checked IND-CCA security and correctness of ML-KEM in EasyCrypt. Crypto 2024. https://eprint.iacr.org/2024/843
- ► Barbosa and Schwabe. **Kyber terminates**. Polynesian Journal of Mathematics. https://eprint.iacr.org/2023/708
- ► Barbosa, Kannwischer, Lim, Schwabe, and Strub. Formally Verified Correctness Bounds for Lattice-Based Cryptography. ACM CCS 2025. https://eprint.iacr.org/2025/1562

Learn even more



Papers related to high-assurance ML-KEM (2/2)

- ► Ammanaghatta Shivakumar, Barthe, Grégoire, Laporte, Oliveira, Priya, Schwabe, and Tabary-Maujean. Typing High-Speed Cryptography against Spectre v1. IEEE S&P 2023. https://eprint.iacr.org/2022/1270
- ► Arranz Olmos, Barthe, Gonzalez, Grégoire, Laporte, Léchenet, Oliveira, and Schwabe. High-assurance zeroization., CHES 2024. https://eprint.iacr.org/2023/1713
- Arranz-Olmos, Barthe, Grégoire, Jancar, Laporte, Oliveira, and Schwabe. Let's DOIT: Using Intel's Extended HW/SW Contract for Secure Compilation of Crypto Code. CHES 2025. https://eprint.iacr.org/2025/759
- ► Arranz Olmos, Barthe, Chuengsatiansup, Grégoire, Laporte, Oliveira, Schwabe, Yarom, and Zhang. Protecting Cryptographic Code Against Spectre-RSB (and, in Fact, All Known Spectre Variants). ASPLOS 2025. https://eprint.iacr.org/2024/1070