



Engineering Post-Quantum Cryptography

May 4, 2022

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· Since 2013: Nijmegen



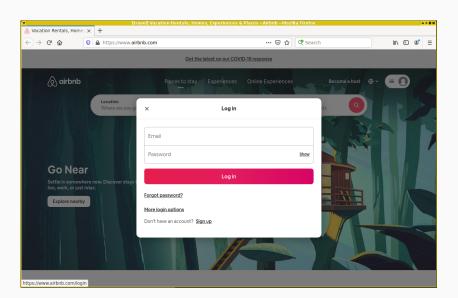
Since Sep. 2020: MPI-SP

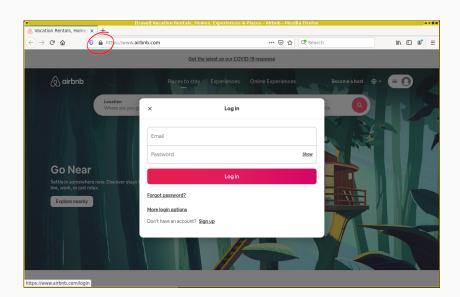


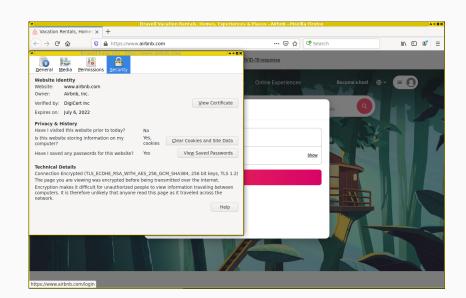
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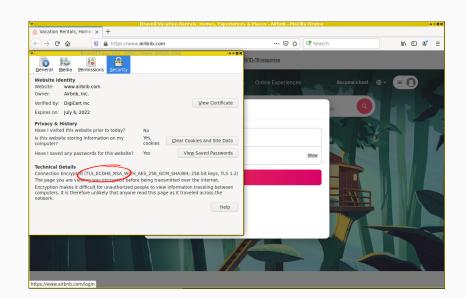
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Polynomial-Time Algorithms for Prime Factorization and Discrete Logarithms on a Quantum Computer*

Peter W. Shor[†]

Abstract

A digital computer is generally believed to be an efficient universal computing device; that is, it is believed able to simulate any physical computing device with an increase in computation time by at most a polynomial factor. This may not be true when quantum mechanics is taken into consideration. This paper considers factoring integers and finding discrete logarithms, two problems which are generally thought to be hard on a classical computer and which have been used as the basis of several proposed cryptosystems. Efficient randomized algorithms are given for these two problems on a hypothetical quantum computer. These algorithms take a number of steps polynomial in the input size, e.g., the number of digits of the integer to be factored.

"In the past, people have said, maybe it's 50 years away, it's a dream, maybe it'll happen sometime. I used to think it was 50. Now I'm thinking like it's 15 or a little more. It's within reach. It's within our lifetime. It's going to happen."

-Mark Ketchen (IBM), Feb. 2012, about quantum computers

Post-quantum crypto

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Post-quantum crypto is (asymmetric) crypto that resists attacks using classical *and quantum* computers.

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5 main directions

- · Lattice-based crypto (PKE and Sigs)
- Code-based crypto (mainly PKE)
- Multivariate-based crypto (mainly Sigs)
- Hash-based signatures (only Sigs)
- Isogeny-based crypto (so far, mainly PKE)

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- · PQC project:
 - · Announcement: Feb 2016
 - · Call for proposals: Dec 2016 (based on community input)
 - · Deadline for submissions: Nov 2017

The NIST competition: initial overview

Count of Problem Category	Column Labels		
Row Labels	Key Exchange	Signature	Grand Total
?	1		1
Braids	1	1	2
Chebychev	1		1
Codes	19	5	24
Finite Automata	1	1	2
Hash		4	4
Hypercomplex Numbers	1		1
Isogeny	1		1
Lattice	24	4	28
Mult. Var	6	7	13
Rand. walk	1		1
RSA	1	1	2
Grand Total	57	23	80
Ç 4	1 31		

Overview tweeted by Jacob Alperin-Sheriff on Dec 4, 2017.

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Signature schemes

- · 3 lattice-based
- 2 symmetric-crypto based
- 4 MQ-based

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- 4 key-agreement schemes
 - · 3 lattice-based
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- · 3 signature schemes
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Alternate schemes

- 5 key-agreement schemes
 - · 2 lattice-based
 - · 2 code-based
 - · 1 isogeny-based
- 3 signature schemes
 - 2 symmetric-crypto based
 - 1 MQ-based

"Yes - the 3rd round will shortly be ending. NIST is actively writing the 3rd Round report which will explain our rationale for which algorithms we will standardize. We hope to be able to announce the results and report not later than the end of March."

-Dustin Moody (NIST), Feb 9, 2022

"We wanted to give another quick update.

We've received a few inquiries about whether NIST's talk at the PKC conference next week will be where we announce the candidates we will select for standardization. The short answer is no - it will not be.

We are still hoping to make our announcement by the end of this month (March)."

-Dustin Moody (NIST), Mar 4, 2022

"Another update:

We had been hoping to announce the results of our PQC standardization process by the end of March. We ask for a little bit more patience since we are not ready to make the announcement today. We still expect to make it very soon."

-Dustin Moody (NIST), Mar 31, 2022

"Everybody,

We appreciate your patience. The announcement of the algorithms we will standardize is still coming very soon. This is a major milestone of our project, and the delay is not due to technical considerations but is due to some legal and procedural steps that are taking more time than we anticipated. Again, thank you for your patience."

-Dustin Moody (NIST), Apr 19, 2022

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Mission accomplished - The world is safe again!

... or is it?

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Replacing MD5 was "easy"!

Challenge 1: Performance



- 10% performance difference matters!
 - · Reduce cost for busy servers
 - · Fit into constrained devices





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 - · Reduce cost for busy servers
 - · Fit into constrained devices
- · Small routines executed many times
- Often hand-optimized on assembly level





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- SPHINCS⁺ signing: ≈3 billion cycles
- Kyber (all ops): <80 kcycles
- Kyber data sent: <1.2 KB

Security reductions

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- · "hard problem" may turn out to be easier than expected
- · proofs may be wrong

The case of OCB2

- 2004: Rogaway proposes OCB2
 - Security reduction guaranteeing confidentiality and authenticity
- 2009: OCB2 is standardized by ISO
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Some NIST PQC proof failures

· Round-1 Kyber proof does not apply

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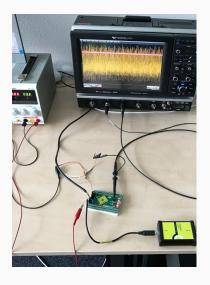
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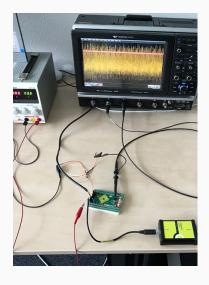
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- · Round-1 Kyber proof does not apply
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- Round-2 qTesla proof wrong (?) ⇒ devastating attack

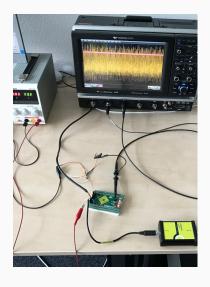




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- · Side-channel attacks:
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 - · Use to obtain secret data
- Timing attacks can be done remotely
- Cost of countermeasures heavily depends on the scheme

"the implementation security aspect of lattice-based cryptography is still a vastly unexplored and open topic"

- Primas, Pessl, Mangard, 2017.

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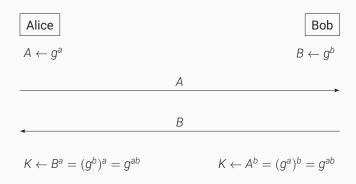
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Challenge 3: Implementation Security (ctd.)

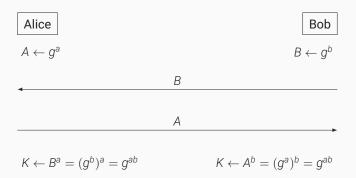
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For many applications, implementations are not ready.

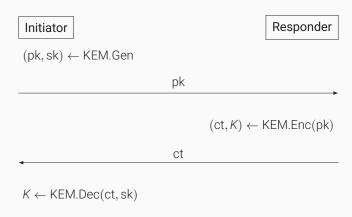
Challenge 4: The curious case of Diffie-Hellman



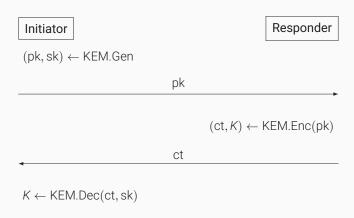
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KEMs: as close as you'll get to DH



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^{*}Except with CSIDH (Castryck, Lange, Martindale, Renes, Panny, 2018)

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"It's a huge foot cannon" — Adam Langley

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How long do we need today's communication to be secure?

How long does it take us to migrate?

But for signatures we have time, right?

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- · Will we know when, say, NSA has a quantum computer?
- May need to prepare devices today!
- · Signatures are used for, e.g., software updates
- · What if I cannot update anymore in 15 years?
 - · What's the lifetime of a car?
 - What's the lifetime of smart-home appliances?

Plan for today

Lattice-based KEMs

- · Intro lecture
- Programming exercise

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Lattice-based KEMs

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Hash-based signatures

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